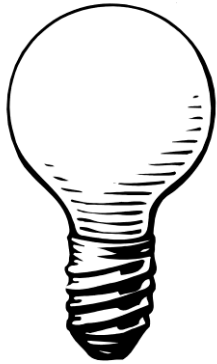


# Numerical Modeling of the Bistability of Electrolyte Transport in Conical Nanopores

Long Luo  
The White Group  
Department of Chemistry  
University of Utah

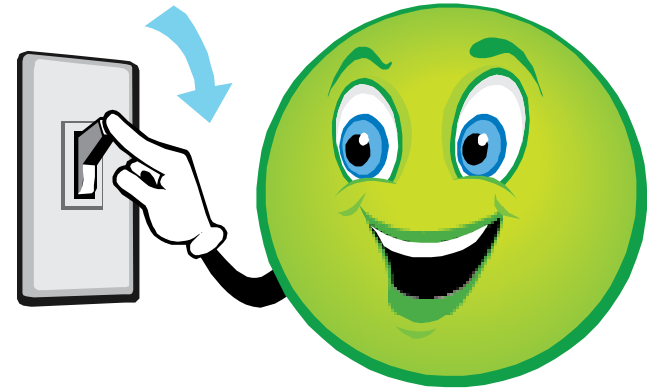
# Bistability



Off

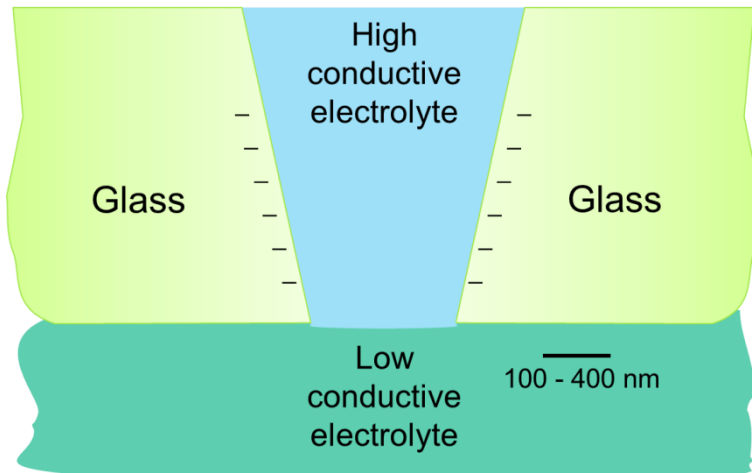


On

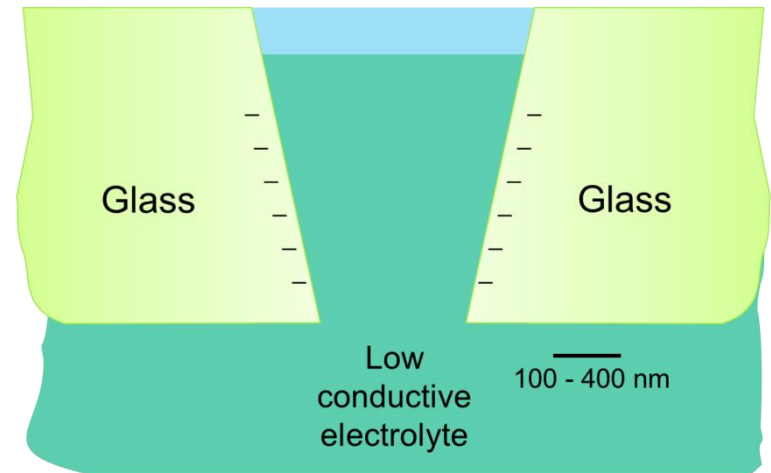


Critical  
condition

# Electrolyte Transport Bistability

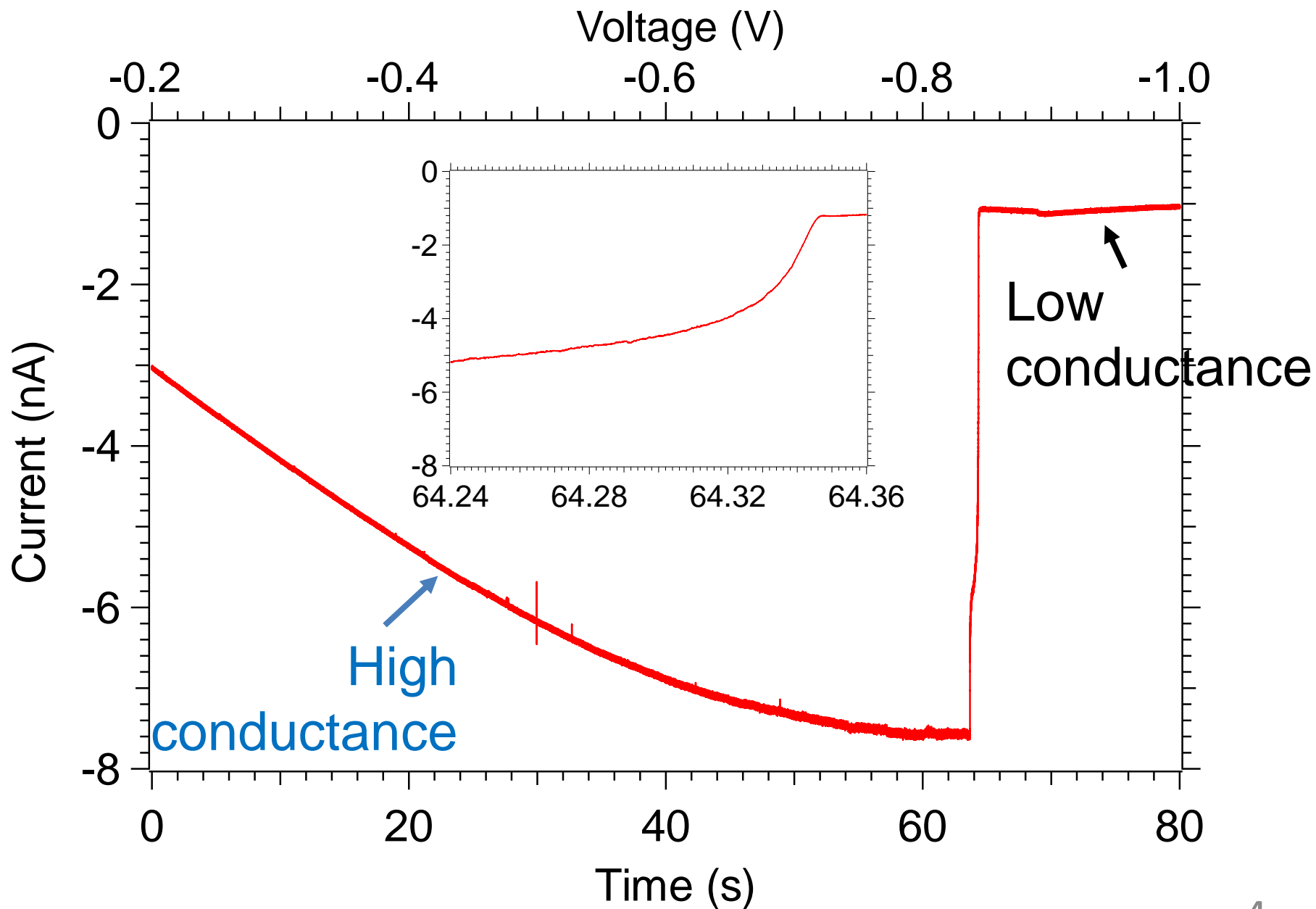


High conductance state  
(HCS)



Low conductance state  
(LCS)

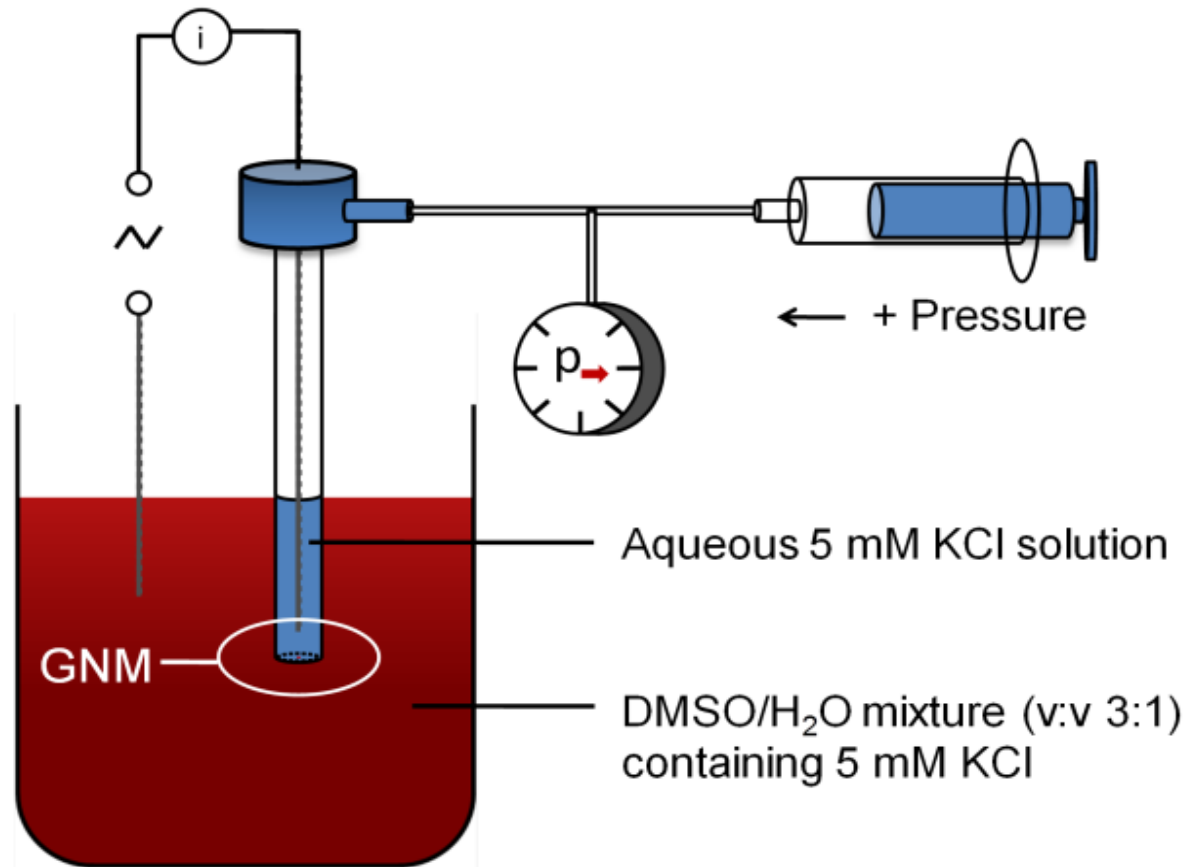
Critical voltage



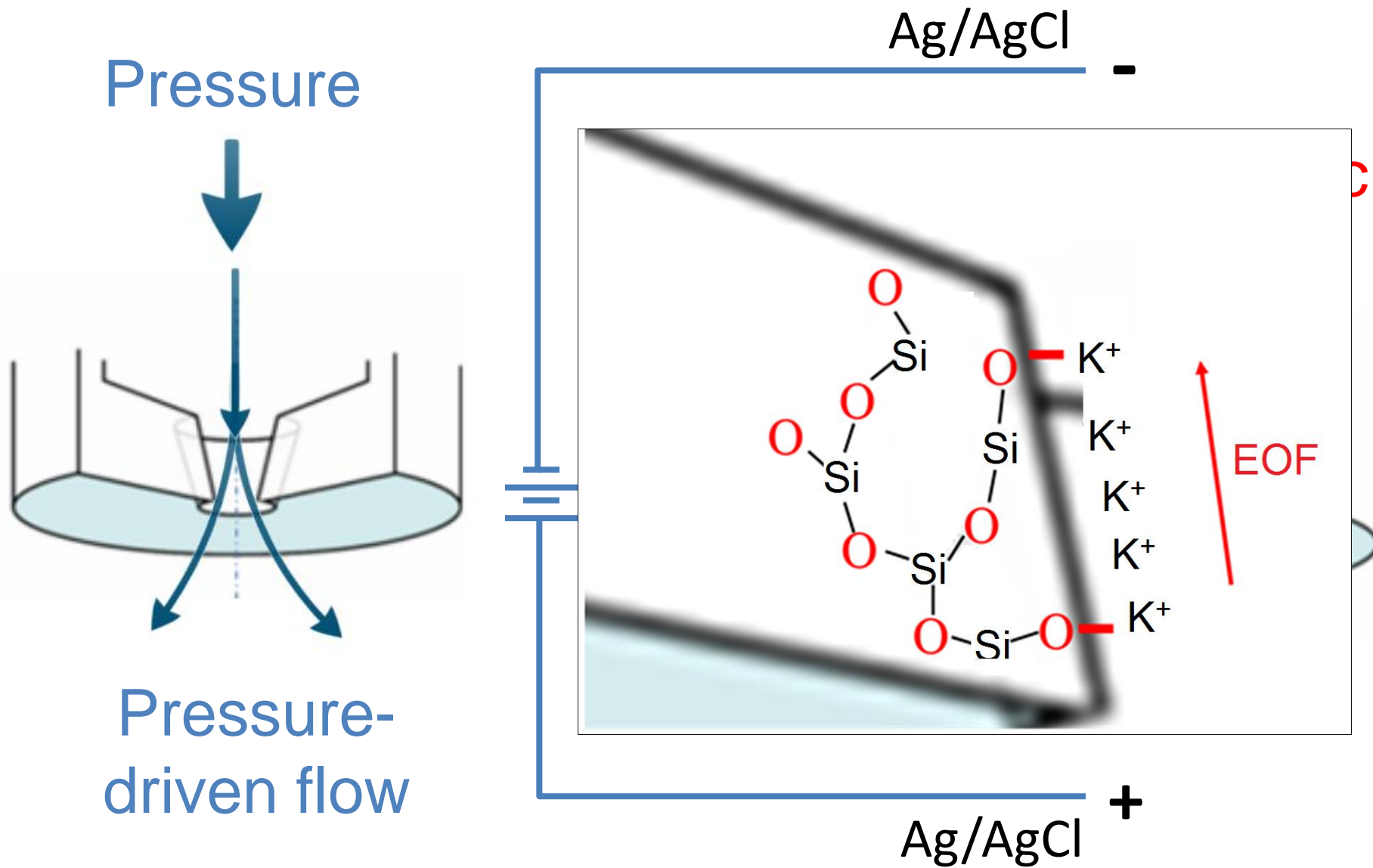
# Experimental Design



**Glass Nanopore Membrane (GNM)**  
Orifice radius:  
200-500 nm

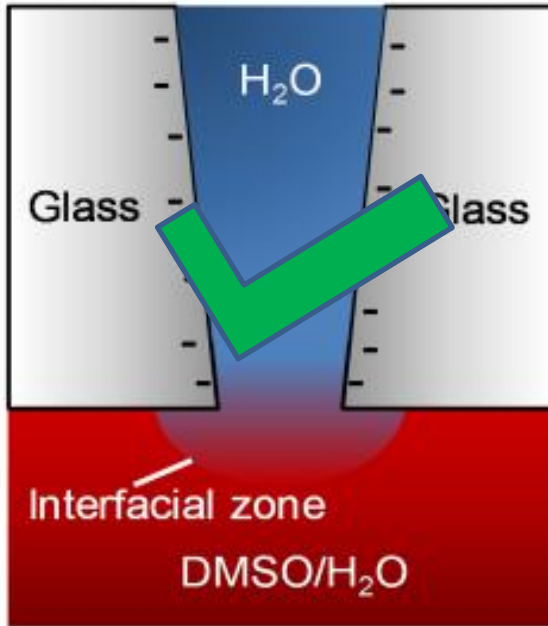


# Experimental Design



# Electrolyte Transport Bistability

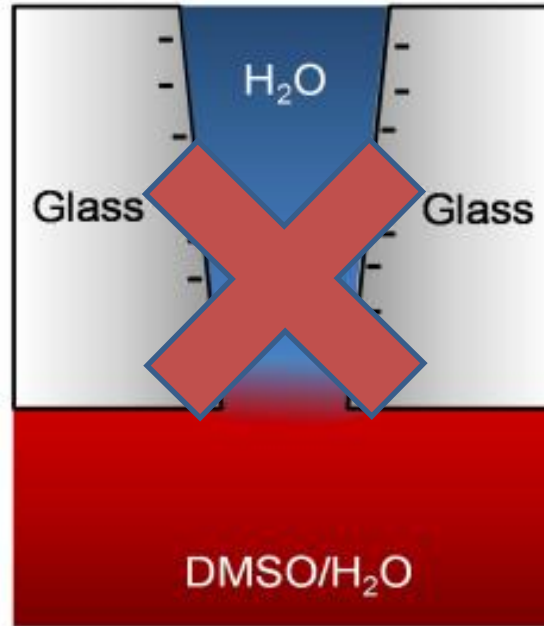
(a)



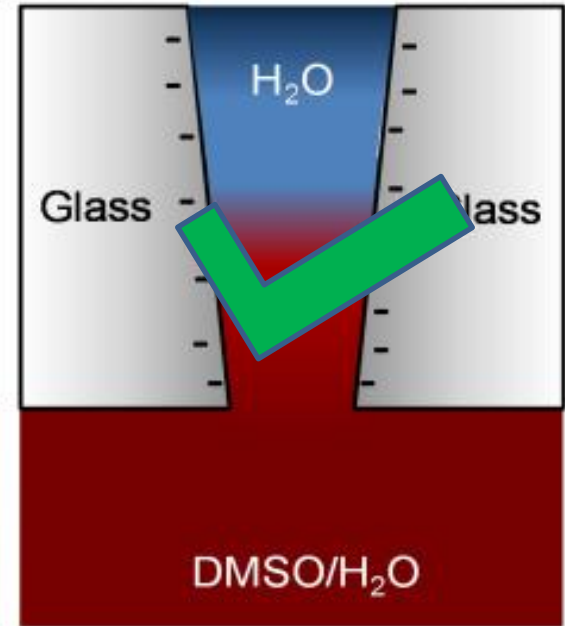
**Stable**

High conductance state  
(HCS)

(b)

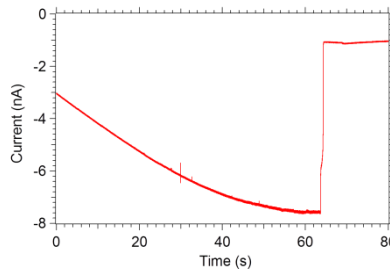


(c)

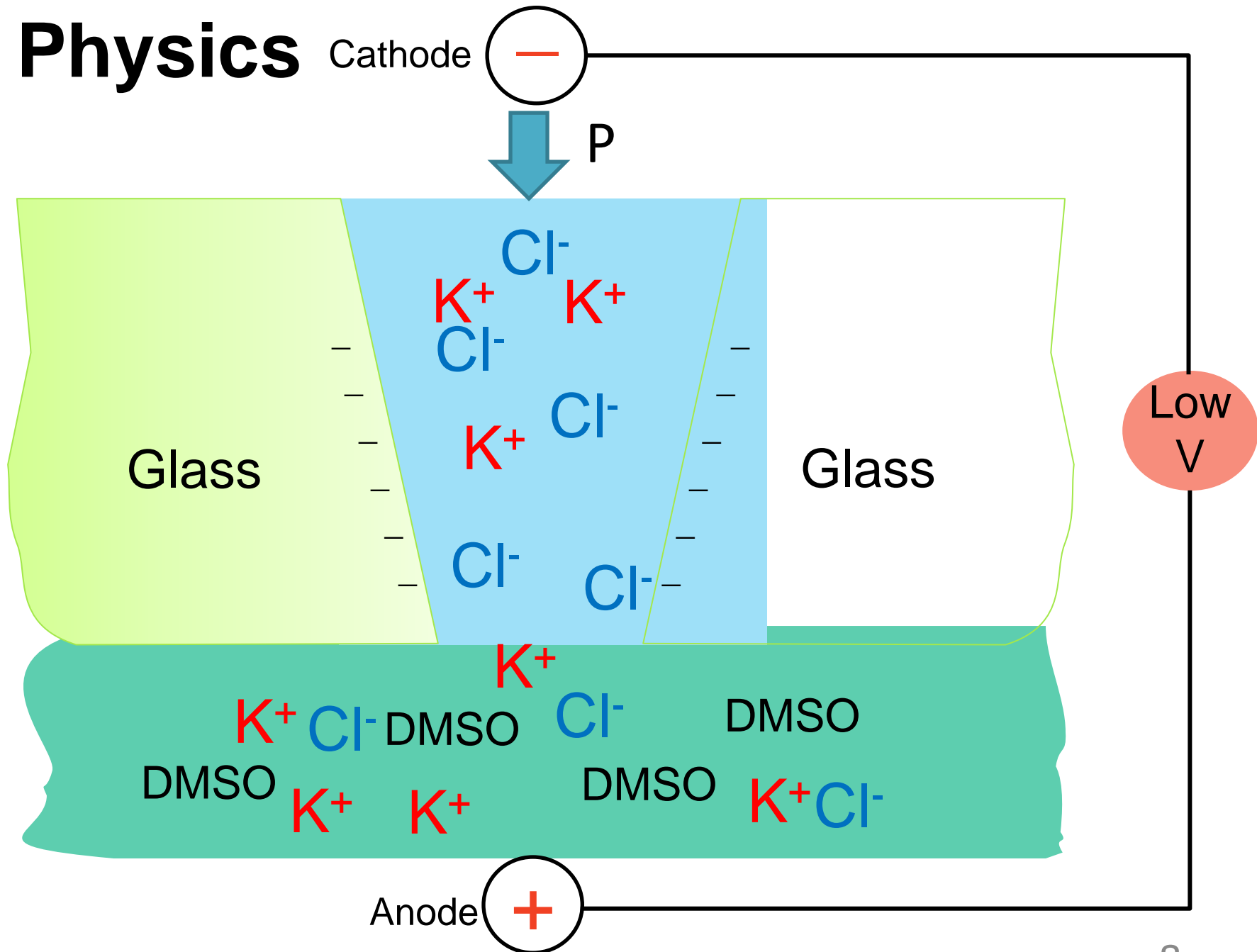


**Stable**

Low conductance state  
(LCS)

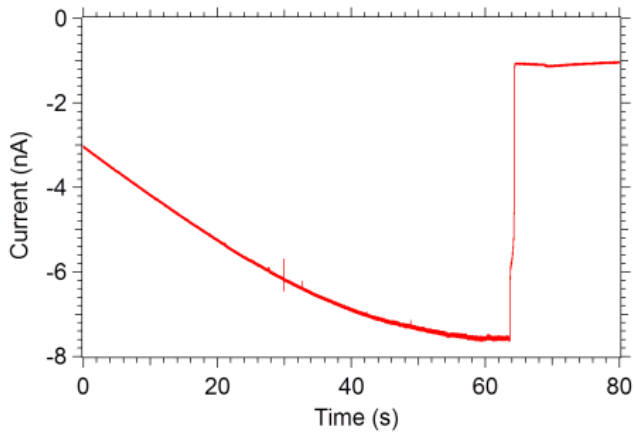
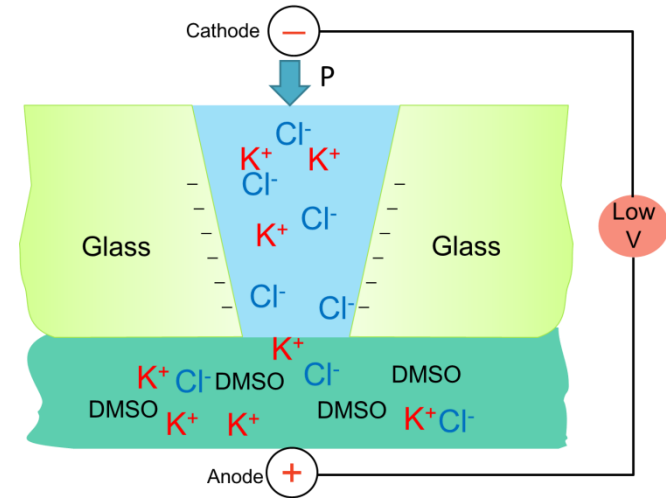


# Physics





# Physics



The goal:  
 $i-V$

The Flux of  
 $K^+$  and  $Cl^-$

DMSO  
Distribution

Laminar  
flow

# COMSOL Model

1) Laminar flow

$$\mathbf{u}\nabla\mathbf{u} = \frac{1}{\rho}(-\nabla p + \eta\nabla^2\mathbf{u} - F(\sum_i z_i c_i)\nabla\Phi)$$

2) Mass transfer

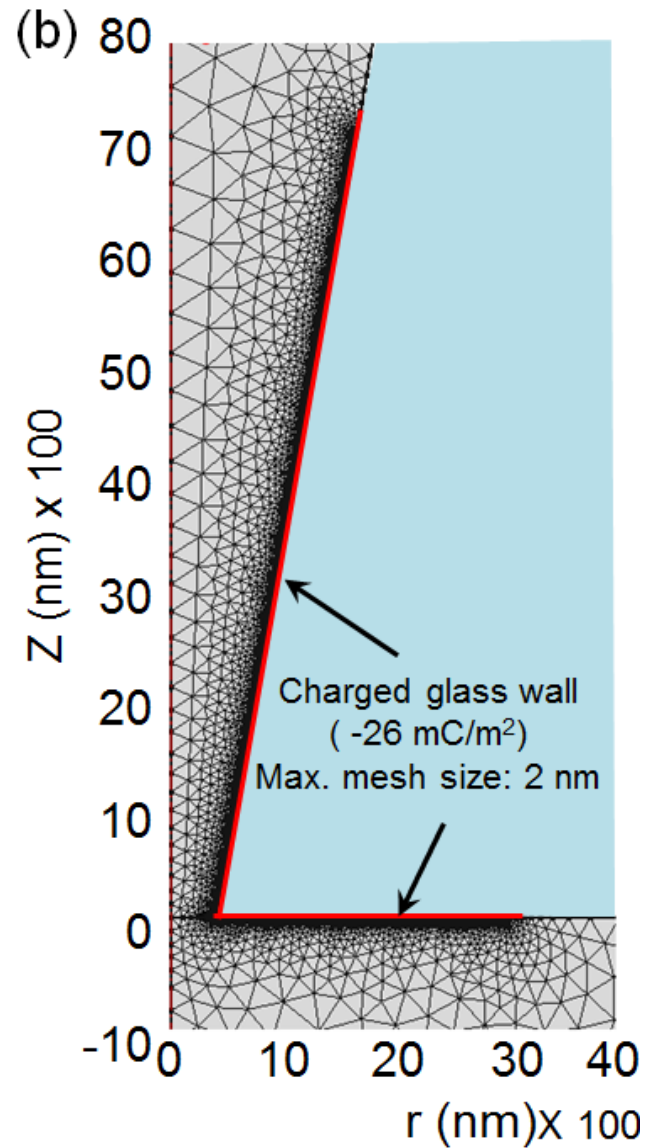
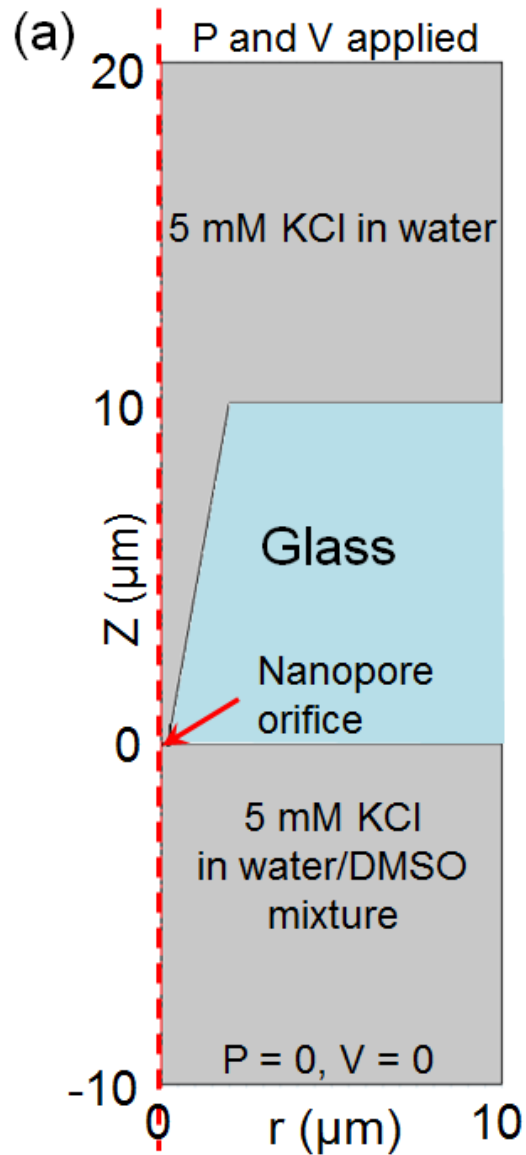
$$\mathbf{J}_i = -D_i\nabla c_i - \frac{Fz_i}{RT}D_i c_i\nabla\Phi + c_i\mathbf{u}$$

$$\mathbf{J}_{DMSO} = -D_{DMSO}\nabla c_{DMSO} + c_{DMSO}\mathbf{u}$$

3) Electrostatics

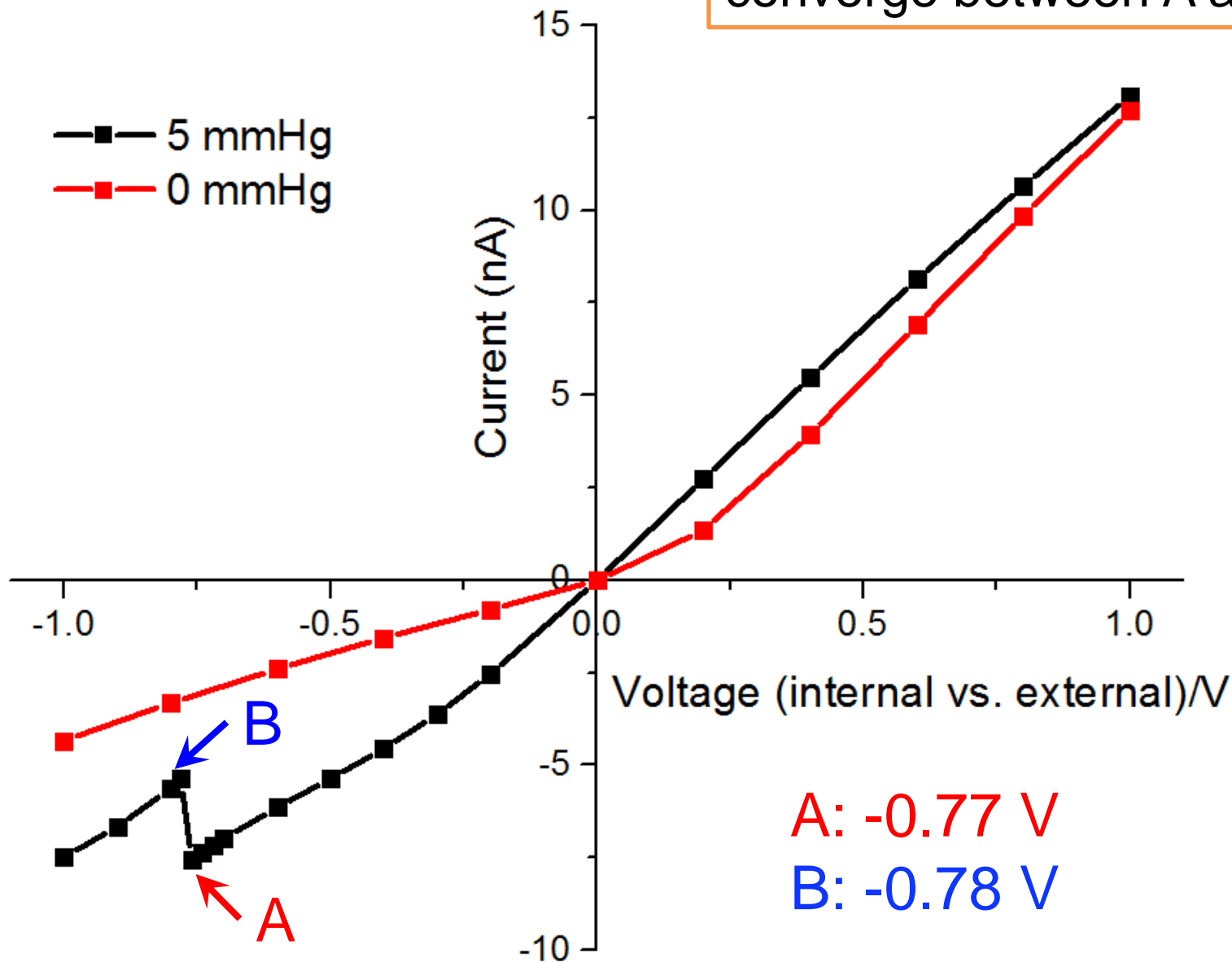
$$\nabla^2\Phi = -\frac{F}{\varepsilon}\sum_i z_i c_i$$

# Geometry and Mesh

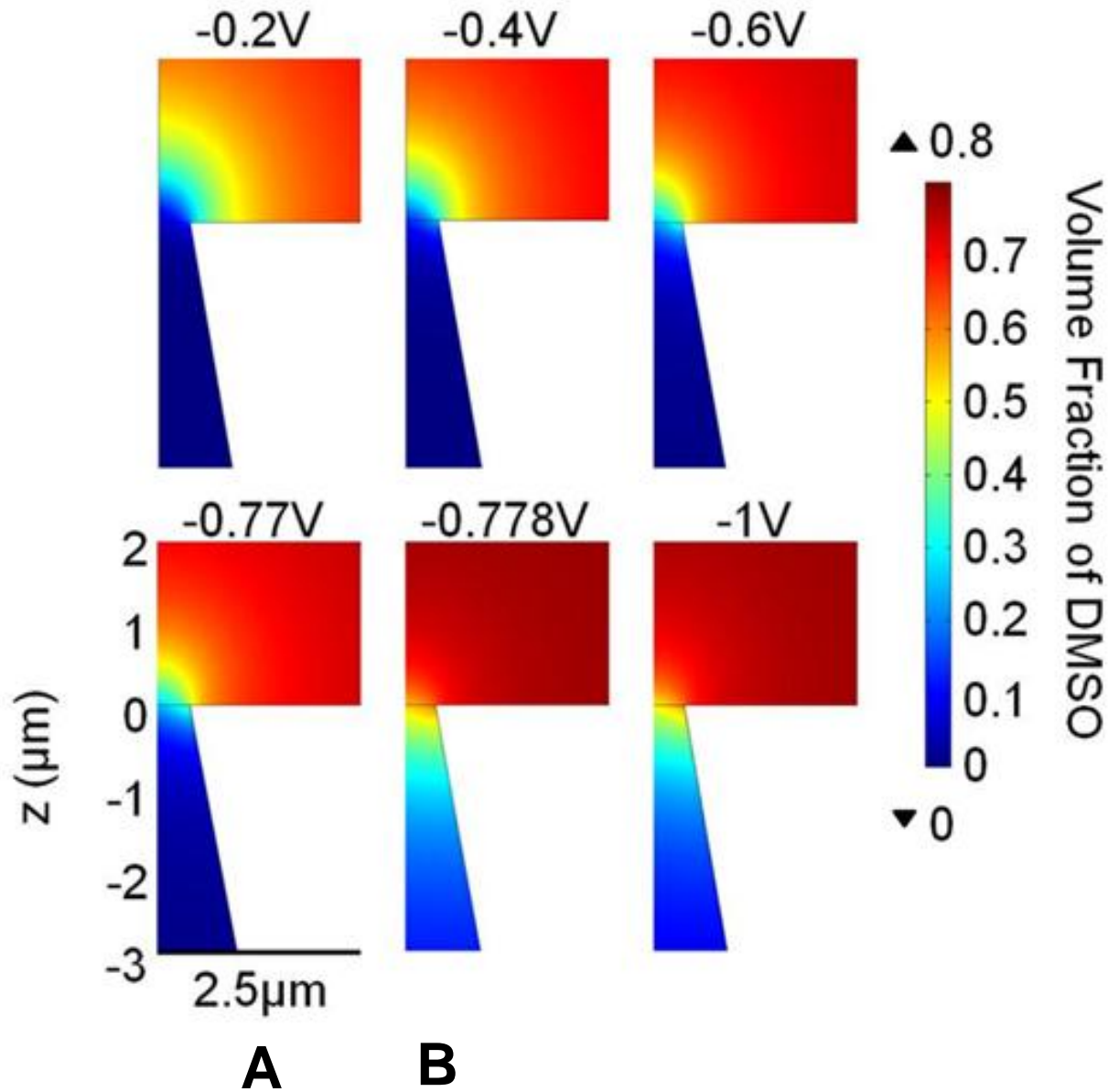


# Simulation Results

The model doesn't converge between A and B!

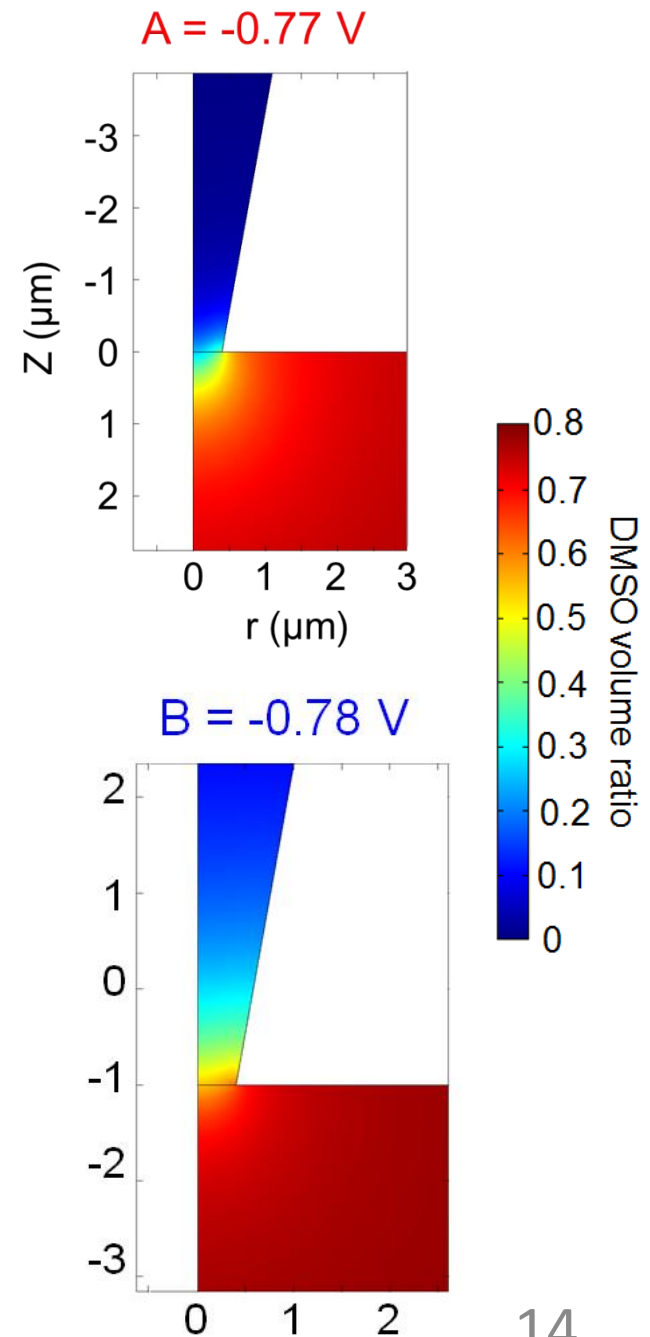
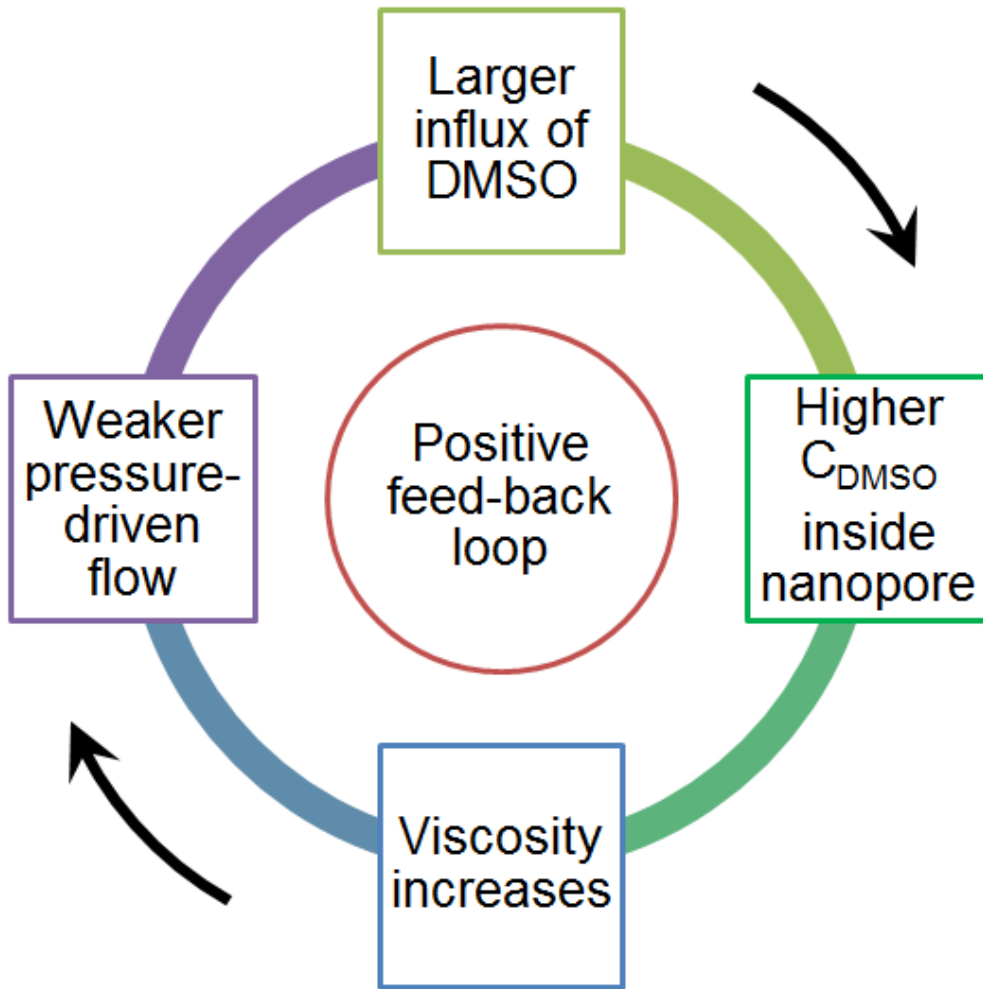


# DMSO Distribution



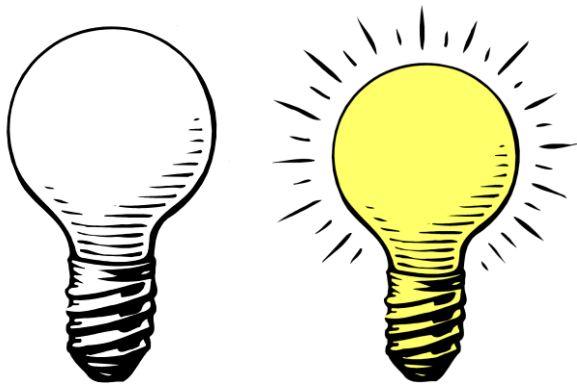
# Mechanism

## Positive feedback loop



# The key point

Bistability



Steady State Solver

Off

On

Thanks for your attentions!

